Loose Primary School Cracking Calculations Session 1 Addition and Subtraction

Information Session For Parents 17.6.2016



Welcome

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Session aims:

- To gain an insight into how addition and subtraction is taught from Year R to Year 6 in school.
- To give ideas for supporting maths at home making it fun!



Addition and Subtraction

The national curriculum for mathematics aims to ensure that all pupils:

- become fluent through varied and frequent practice with increasingly complex problems over time
- can solve problems by applying their mathematics to a variety of routine and nonroutine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions.



What method would you use?

17 + 23 =

349 + 278 =

1998 + 567 =

185 – 35 =

2005 - 1997 =

3485 - 2876 =

Mental and written strategies

As pupils progress through the school it is vital that we develop their mental strategies as well as their ability to record using a written method.

Strategies for teaching mental addition include:

• Putting the largest number first: 5 + 36 is the same as 36 + 5. Start at 36 and count on in ones 30 + 60 is the same as 60 + 30. Start at 60 and count on in tens

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• Partitioning:

14 + 25 = (10 + 4) + (20 + 5)

(10 + 20) = 30

(4 + 5) = 9

The answer is 39
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Compensation:
17 + 9 = 17 + 10 - 1 = 26
26 + 11 = 26 + 10 + 1 = 37
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    Doubles or near doubles:
    8 + 8 = 16
    8 + 9 = 8 + 8 + 1 = 17
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Bridging through 10, 20, etc...
8 + 7 = (8 + 2) + 5
10 + 5 = 15
15 + 9 = (15 + 5) + 4
20 + 4 = 24
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Year R

In their first year at Loose, pupils will develop their awareness of number.

By the end of the year, the majority of pupils will be able to:

- Recognise and order numbers to 20, as well as identify one more or one less than any number up to 10.
- add and subtract two single-digit numbers and count on or back to find the answer using practical equipment for support.



Year R - Addition

Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

GUIDANCE / MODELS AND IMAGES	KEY VOCABULARY
If available, Numicon shapes are introduced straight away and can be used to: • identify 1 more/less • combine pieces to add. • find number bonds. • add without counting. Children can record this by printing or drawing around Numicon pieces.	Games and songs can be a useful way to begin using vocabulary involved in addition e.g. Alice the Camel
Children begin to combine groups of objects using concrete apparatus +	add more
Construct number sentences verbally or using cards to go with practical activities.	and
Children are encouraged to read number sentences aloud in different ways "Three add two equals 5""5 is equal to three and two"	make sum
Children make a record in pictures, words or symbols of addition activities already carried out.	total altogether
Solve simple problems using fingers	score
5+1=6	double
Number tracks can be introduced to count up on and to find one more:	one more, two more, ten more
Number lines can then be used alongside number tracks and practical apparatus to 5+3=8 solve addition calculations and word problems.	how many more to make?
Children will need opportunities to look at and talk about different models and images as they move between representations.	how many more is than?



Year R - Subtraction

Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

GUIDANCE / MODELS AND IMAGES		KEY VOCABULARY
Children begin with mostly pictorial representations		Games and songs can be
xxx XX		a useful way to begin using vocabulary
000		involved in subtraction
		e.g.
Concrete apparatus is used to relate subtraction to taking away and counting how many	• • • • <u>×</u>	Five little men in a flying
objects are left.	5 - 1 = 4	saucer
Concrete apparatus models the subtraction of 2 objects from a set of 5.		
Construct number sentences verbally or using cards to go with practical activities.		take (away)
Children are encouraged to read number sentences aloud in different ways "five subtract one leaves four" "four is		leave
equal to five subtract one"		how many are left/left
	over?	
Children make a record in pictures, words or symbols of subtraction activities already carried out.		
Solve simple problems using fingers		how many have gone?
		one less, two less ten less
5 - 1 = 4		
Number tracks can be introduced to count back and to find one less:		how many fewer is
What is 1 less than 9? 1 less than 20?		than?
Number lines can then be used alongside number tracks and practical	difference between	
apparatus to solve subtraction calculations and word problems. Children	is the same as	
count back under the number line.		
Children will need opportunities to look at and talk about different models and images as they n representations.	nove between	



Years 1 and 2

- The principal focus of mathematics teaching in Key Stage 1 is to ensure that pupils develop confidence and mental fluency with whole numbers, counting and place value.
- By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value. An emphasis on practice at this early stage will aid fluency.



Years 3 to 6

- The principal focus of mathematics teaching in lower Key Stage 2 is to ensure that pupils become increasingly fluent with whole numbers and the four operations, including number facts and the concept of place value.
- Once they reach upper Key Stage 2, pupils should develop their ability to solve a wider range of problems, including increasingly complex properties of numbers and arithmetic, and problems demanding efficient written and mental methods of calculation. With this foundation in arithmetic, pupils are introduced to the language of algebra as a means for solving a variety of problems.



Addition Progression in written methods



Year 1	Year 2	Year 3
+ = signs and missing numbers Children need to understand the concept of equality	Missing number problems e.g 14 + 5 = 10 + 32 + + = 100 35 = 1 + + 5	Missing number problems using a range of equations as in Year 1 and 2 but with appropriate, larger numbers.
before using the '=' sign. Calculations should be written either side of the equality sign so that the sign is not just interpreted as 'the answer'. 2 = 1+ 1 2 + 3 = 4 + 1	It is valuable to use a range of representations (also see Y1). Continue to use numberlines to develop understanding of: $\frac{\text{Counting on in tens and ones}}{23 + 12 = 23 + 10 + 2}$	Partition into tens and ones Partition both numbers and recombine. Count on by partitioning the second number only e.g. 247 + 125 = 247 + 100 + 20 + 5 = 347 + 20 + 5
Missing numbers need to be placed in all possible places. $3 + 4 = \Box$ $\Box = 3 + 4$ $3 + \Box = 7$ $7 = \Box + 4$	= 35233335Partitioning and bridging through 10.The steps in addition often bridge through a multiple of 10e.g. Children should be able to partition the 7 to relate adding the2 and then the 5.	= 367 + 5 = 372 Children need to be secure adding multiples of 100 and 10 to any three-digit number including those that are not multiples of 10.
Counting and Combining sets of Objects Combining two sets of objects (aggregation) which will progress onto adding on to a set (augmentation)	$8 + 7 = 15$ $4dding 9 \text{ or } 11 \text{ by adding } 10 \text{ and adjusting by } 1$ $a \neq Add 9 \text{ by adding } 10 \text{ and adjusting by } 1$	Towards a Written Method Introduce expanded column addition modelled with place value counters (Dienes could be used for those who need a less abstract representation)
	35 + 9 = 44 $35 + 9 = 44$ -1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Understanding of counting on with a number track.	Towards a Written Method Partitioning in different ways and recombine 47+25	+ <u>125</u> + <u>125</u> 12 10 10 60
(supported by models and images).	47 25 60 + 12	Leading to children understanding the exchange
7+4 0 1 2 3 4 5 6 7 8 9 10 11 12	Leading to exchanging:	between tens and ones.
		Some children may begin to use a formal columnar algorithm, initially introduced alongside the expanded
	Expanded written method $40 + 7$ $40 + 7 + 20 + 5 =$ $+ 20 + 5$ $40+20+7+5 =$ $60 + 12 = 72$	method. The formal method should be seen as a more streamlined version of the expanded method, not a new method. $\begin{array}{r} 247 \\ \underline{+125} \\ \underline{372} \\ 10 \end{array}$

Year 4	Year 5	Year 6
Missing number/digit problems:	Missing number/digit problems:	Missing number/digit problems:
Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving. Written methods (progressing to 4-digits) Expanded column addition modelled with place value counters, progressing to calculations with 4-digit numbers. $ \begin{array}{c} $	Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving. Children should practise with increasingly large numbers to aid fluency e.g. 12462 + 2300 = 14762 Written methods (progressing to more than 4-digits) As year 4, progressing when understanding of the expanded method is secure, children will move on to the formal columnar method for whole numbers and decimal numbers as an efficient written algorithm. 172.83 + 54.68 227.51 1 1 1 Place value counters can be used alongside the columnar method to develop understanding of addition with decimal numbers.	Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving. Mritten methods As year 5, progressing to larger numbers, aiming for both conceptual understanding and procedural fluency with columnar method to be secured. Continue calculating with decimals, including those with different numbers of decimal places Problem Solving Teachers should ensure that pupils have the opportunity to apply their knowledge in a variety of contexts and problems (exploring cross curricular links) to deepen their understanding.

Subtraction Progression in written methods



Year 1	Year 2	Year 3
Missing number problems e.g. $7 = -9; 20 - 0 = 9;$ 15 - 9 = 0; 0 - 0 = 11; 16 - 0 = 0 Use concrete objects and pictorial representations. If appropriate, progress from using number lines with every number shown to number lines with significant numbers shown. Understand subtraction as take-away:	Missing number problems e.g. $52 - 8 = \Box; \Box - 20 = 25; 22 = \Box - 21; 6 + \Box + 3 = 11$ It is valuable to use a range of representations (also see Y1). Continue to use number lines to model take-away and difference. E.g. 25 27 37 -2 $-10+1$ $+239$ 40 $42The link between the two may be supported by an image like this, with 47 being taken away from 72, leaving the difference, which is 25.+3$ $+20$ $+20$ -70 70 $72The bar model should continue to be used, as well as images in the context of measures.Towards written methodsRecording addition and subtraction in expanded columns can support understanding of the quantity aspect of place value and prepare for efficient written methods with larger numbers. The numbers may be represented with Dienes apparatus. E.g. 75 - 42$	Missing number problems e.g. $= 43 - 27$; $145 - = 138$; $274 - 30 = = 245 - = 195$; $532 - 200 = = 364 - 153 = =$ Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving (see Y1 and Y2). Children should make choices about whether to use complementary addition or counting back, depending on the numbers involved. Written methods (progressing to 3-digits) Introduce expanded column subtraction with no decomposition, modelled with place value counters (Dienes could be used for those who need a less abstract representation) $90 \ 8 \ - 30 \ 5 \ 60 \ 3$ For some children this will lead to exchanging, modelled using place value counters (or Dienes). $90 \ 8 \ - \frac{30 \ 5}{60 \ 3}$ For some children this will lead to exchanging, modelled using place value counters (or Dienes). $90 \ 8 \ - \frac{76 \ 2}{20 \ 5}$ A number line and expanded column method may be compared next to each other.
to pictorial representation. The use of other images is also valuable for modelling subtraction e.g. Numicon, bundles of straws, Dienes apparatus, multi-link cubes, bead strings		Some children may begin to use a formal columnar algorithm, initially introduced alongside the expanded method. The formal method should be seen as a more streamlined version of the expanded method, not a new

method.

Year 4	Year 5	Year 6
Missing number/digit problems: $456 + \Box = 710$; $1\Box 7 + 6\Box = 200$; $60 + 99 + \Box = 340$; $200 - 90 - 80 = \Box$; $225 - \Box = 150$; $\Box - 25 = 67$; $3450 - 1000 = \Box$; $\Box - 2000 = 900$ Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving. Written methods (progressing to 4-digits) Expanded column subtraction with decomposition, modelled with place value counters, progressing to calculations with 4-digit numbers. $100 \ 10 \ 4$ $100 \ 10 \ 8$ If understanding of the expanded method is secure, children will move on to the formal method of decomposition, which again can be initially modelled with place value counters. 2322 - 1114	Missing number/digit problems: $6.45 = 6 + 0.4 + \Box$; $119 - \Box$ = 86; 1 000 000 - \Box = 999 000; 600 000 + \Box + 1000 = 671 000; 12 462 - 2 300 = \Box Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving. Written methods (progressing to more than 4-digits) When understanding of the expanded method is secure, children will move on to the formal method of decomposition, which can be initially modelled with place value counters.	Missing number/digit problems: \Box and # each stand for a different number. # = 34. # + # = \Box + \Box + #. What is the value of \Box ? What if # = 28? What if # = 21 10 000 000 = 9 000 100 + \Box 7 - 2 x 3 = \Box ; (7 - 2) x 3 = \Box ; (\Box - 2) x 3 = 15 Mental methods should continue to develop, supported by a range of models and images, including the number line. The bar model should continue to be used to help with problem solving. Written methods As year 5, progressing to larger numbers, aiming for both conceptual understanding and procedural fluency with decomposition to be secured. Teachers may also choose to introduce children to other efficient written layouts which help develop conceptual understanding. For example: 326 - <u>148</u> -2 -20 <u>200</u> <u>178</u>
• • <u>• 118</u>	Progress to calculating with decimals, including those with different numbers of decimal places.	Continue calculating with decimals, including those with different numbers of decimal places.

Mental methods - Addition

Addition

Year 4	Year 5	Year 6
Mental Strategies	Mental Strategies	Mental Strategies
Children should continue to count regularly, on and back, now including multiples of 6, 7, 9, 25 and 1000, and steps of 1/100. The number line should continue to be used as an	Children should continue to count regularly, on and back, now including steps of powers of 10. The number line should continue to be used as an important image to support thinking, and the use of informal jottings	Consolidate previous years. Children should experiment with order of operations,
important image to support thinking, and the use of informal jottings should be encouraged where appropriate.	should be encouraged where appropriate. Children should continue to partition numbers in different ways.	investigating the effect of positioning the brackets in different places, e.g. $20 - 5 \times 3 = 5$; $(20 - 5) \times 3 = 45$
Children should continue to partition numbers in different ways.		
They should be encouraged to choose from a range of	 They should be encouraged to choose from a range of strategies: Counting forwards and backwards in tenths and 	
 strategies: Counting forwards and backwards: 124 – 47, count back 40 from 124, then 4 to 80, then 3 to 77 Reordering: 28 + 75, 75 + 28 (thinking of 28 as 25 + 3) Partitioning: counting on or back: 5.6 + 3.7, 5.6 + 3 + 0.7 = 8.6 + 0.7 Partitioning: bridging through multiples of 10: 6070 – 4987, 4987 + 13 + 1000 + 70 Partitioning: compensating – 138 + 69, 138 + 70 - 1 Partitioning: using 'near' doubles - 160 + 170 is double 150, then add 10, then add 20, or double 160 and add 10, or double 170 and subtract 10 Partitioning: bridging through 60 to calculate a time interval – What was the time 33 minutes before 2.15pm? Using known facts and place value to find related facts. 	 budded the second second and the second se	



Mental methods - Subtraction

Subtraction		
Year 1	Year 2	Year 3
Mental Strategies	Mental Strategies	Mental Strategies
Children should experience <u>regular counting</u> on and back from different numbers in 1s and in multiples of 2, 5 and 10. Children should memorise and reason with number bonds for numbers to 20, experiencing the = sign in different positions. They should see addition and subtraction as related operations. E.g. 7 + 3 = 10 is related to $10 - 3 = 7$, understanding of which could be supported by an image like this.	Children should count regularly, on and back, in steps of 2, 3, 5 and 10. Counting back in tens from any number should lead to subtracting multiples of 10. Number lines should continue to be an important image to support thinking, for example to model how to subtract 9 by adjusting. +1	Children should continue to count regularly, on and back, now including multiples of 4, 8, 50, and 100, and steps of 1/10. The number line should continue to be used as an important image to support thinking, and the use of informal jottings should be encouraged. Children should continue to partition numbers in difference ways. They should be encouraged to choose the mental strategies which are most efficient for the numbers involved, e.g. counting up (difference, or complementary addition) for 201 – 198; counting back (taking away / partition into tens and ones) for 201 – 12.
Use bundles of straws and Dienes to model partitioning teen numbers into tens and ones.	Children should practise subtraction to 20 to become increasingly fluent. They should use the facts they know to derive others, e.g using 10 - 7 = 3 and 7 = 10 - 3 to calculate 100 - 70 = 30 and 70 = 100 - 30.	Calculators can usefully be introduced to encourage fluency by using them for games such as 'Zap' [e.g. Enter the number 567. Can you 'zap' the 6 digit and make the display say 507 by subtracting 1 number?] The strategy of adjusting can be taken further, e.g. subtract 100 and add one back on to subtract 99. Subtract other near multiples of 10 using this
Children should begin to understand subtraction as both taking away and finding the difference between, and should find small differences by counting on. 5 - = 3 = -2 = 3 $3 = -2 = 3$ $3 = -2 = -3$ $3 = -2$	91 92 93 94 95 96 97 90 90 81 92 83 64 85 66 77 78 77 77 77 77 77 77 77 77 77 77 77 77 77 77 77 77 77 78 77 78 79 70 <	strategy. <u>Vocabulary</u> Hundreds, tens, ones, estimate, partition, recombine, difference, decrease, near multiple of 10 and 100, inverse, rounding, column subtraction, exchange See also Y1 and Y2
Subtraction as "the difference between"	They should continue to see subtraction as both take away and hinding the difference, and should find a small difference by counting up. They should use Dienes to model partitioning into tens and ones and learn to partition numbers in different ways e.g. 23 = 20 + 3 = 10 + 13. <u>Vocabulary</u>	
Vocabulary Subtraction, subtract, take away, distance between, difference between, more than, minus, less than, equals = same as, most, least, pattern, odd, even, digit,	ones, partition, near multiple of 10, tens boundary, less than, one less, two less ten less one hundred less, more, one more, two more ten more one hundred more	LOOSE Primary School

Subtraction

Voor A	Voor E	Voor 6
fear 4	Teal 5	fear 6
Mental Strategies	Mental Strategies	Mental Strategies
Children should continue to count regularly, on and back, now including multiples of 6, 7, 9, 25 and 1000, and steps of 1/100.	Children should continue to count regularly, on and back, now including steps of powers of 10.	Consolidate previous years.
The number line should continue to be used as an important image to support thinking, and the use of informal jottings should be encouraged where appropriate. Children should continue to partition numbers in different ways.	The number line should continue to be used as an important image to support thinking, and the use of informal jottings should be encouraged where appropriate. Children should continue to partition numbers in different ways.	Children should experiment with order of operations, investigating the effect of positioning the brackets in different places, e.g. $20 - 5 \times 3 = 5$; $(20 - 5) \times 3 = 45$
They should be encouraged to choose from a range of	They should be encouraged to choose from a range of	<u>Vocabulary</u>
strategies:	strategies:	See previous years
 Counting forwards and backwards: 124 – 47, count back 40 from 124, then 4 to 80, then 3 to 77 Reordering: 28 + 75, 75 + 28 (thinking of 28 as 25 + 3) Partitioning: counting on or back: 5.6 + 3.7, 5.6 + 3 + 0.7 = 8.6 + 0.7 Partitioning: bridging through multiples of 10: 6070 – 4987, 4987 + 13 + 1000 + 70 Partitioning: compensating – 138 + 69, 138 + 70 - 1 Partitioning: using 'near' doubles - 160 + 170 is double 150, then add 10, then add 20, or double 160 and add 10, or double 170 and subtract 10 Partitioning: bridging through 60 to calculate a time interval – What was the time 33 minutes before 2.15pm? Using known facts and place value to find related facts. 	 Counting forwards and backwards in tenths and hundredths: 1.7 + 0.55 Reordering: 4.7 + 5.6 - 0.7, 4.7 - 0.7 + 5.6 = 4 + 5.6 Partitioning: counting on or back - 540 + 280, 540 + 200 + 80 Partitioning: bridging through multiples of 10: Partitioning: compensating: 5.7 + 3.9, 5.7 + 4.0 - 0.1 Partitioning: using 'near' double: 2.5 + 2.6 is double 2.5 and add 0.1 or double 2.6 and subtract 0.1 Partitioning: bridging through 60 to calculate a time interval: It is 11.45. How many hours and minutes is it to 15.20? Using known facts and place value to find related facts. 	
add, addition, sum, more, plus, increase, sum, total,	Also see previous years	
altogether, double, near double, how many more to make? how much more? ones boundary, tens boundary, hundreds boundary, thousands boundary, tenths boundary, hundredths boundary, inverse, how many		Loose Primary School

How can you support at home?

The best thing that parents and carers can do for children is to have a positive attitude towards maths.

Take an interest in their learning and encourage them to be independent learners.

There is lots more helpful information and ideas for activities to play at home on our school website.



Any Questions?

